# CAE FOR HIGH PERFORMANCE IN-FEED PROCESSES AT SORTING SYSTEMS

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Abstract: This paper concludes the first steps for CAE with sorting systems from ICMaS'12. As high performance sorting processes are more and more relevant not only but very much from e-commerce business engineering is addressed to bring faster, more accurate and safer technologies therein. The authors describe the in-feed-process, identified as a crucial one for extending sorter performance. An analytical solution (2D) for the "classic" belt feeder is presented and compared with a multibody model. Valuable insights for modelling, effort and practical use are demonstrated. A MBD-simulation is presented and an overview shows where and how to adjust the design from simulation findings.

*Key words:* CAE, Multi Body Dynamics/Simulation (MBD, MBS), sortation system, tilt tray sorter, in feed process, design optimization, design of experiments.

## 1. INTRODUCTION

Within highly competitive markets nearly every branch based on engineering in whatever way to think successful providers of solutions and products are demanded to improve product quality and lower costs more than competitors. Those different branches, like automotive, aerospace, general machinery and logistics engineering or material handling equipment design have found more or less optimal solutions, to handle these demands in various ways.

Looking about design methodologies and engineering or product development guidelines [7, 8, 9], subsuming over several different approaches one can identify a clear trend to:

- Parallelize engineering tasks.
- Transferring time consuming calculation and simulation task to an early stage in product development (frontloading) to manage costs

altogether named as simultaneous engineering (SE) as shown in a comprehensive view in Fig. 1.

Product development has a clear vision for valid function of the product, which can only be secured in a very late state i.e. detailed design or development (Fig. 1). As building test stands, to verify product functions is depending very much on the final geometry of the product – which is itself a result of the overall design process – is very time consuming and expensive and therefore

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not easily to adapt, one has to find other ways to demonstrate and examine product function.

Therefore Computer-Aided-Engineeing Methods (CAE) are widely spread over the engineering branches as a common way to deal with demands mentioned above. A few key performance indicators can be identified, describing CAE in engineering:

- Highly adaptable modelling (geometry, mechanical parameters).
- Various different ways, to "examine" and use a model by scaling sizes and varying parameters; Design of Experiments (DoE).
- Once basic knowledge is achieved and a model library is established short and inexpensive development of models can be possible.

Material Handling and Logistics Engineering is not so much driven by virtual engineering as i.e. automotive development. But the impact in reducing test stands, by generating models, simulations and DoE, is quite large, as the test installations are highly complex and not easy to adjust in it's parameters. So the authors and the whole Institute of Logistics Engineering at Graz University of Technology (ITL) have a clear vision, to empower material handling engineering tasks with CAE technology. A conveyor-toolbox is actual state of research, where some details have been presented at ICMaS'12 [6] and is concluded within this work focusing on the in-feed-process in sortation systems and general material handling devices.

## 2. THE SORTATION SYSTEM AND THE IN-FEED

With higher volumes in parcel and piece goods distribution performance of sorting systems is increasing continuously. Those highly engineered products are touching limits of physics, achieving i.e. centripetal forces and frictions hard on the limit. Therefore there is a necessity of CAE and DoE specially for new technologies and high

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Fig. 1. Product Development Process (PEP) with overlapping phases (SE) [2].



**Fig. 2.** A sorting system installation – mechanical view without identification and control [1].

performace systems. With varying throughput, speed, variety of goods the field for CAE and DoE is defined clearly.

A short description of sortation systems helps to understand the overall vision [6]. Sortation systems are found in various installations: Baggage handling in airports, distribution of parcels, mail order business, etc. The core of a sortation system is the sorter itself (Fig. 2), which distributes goods to their specified accumulation area.

Different types of sorting systems are used like Line sorters, loop sorters or ring sorters. In general a sortation system is sub-divided in five different parts (Fig. 3):

- 1: In-feed or induction: goods/parcels enter sorting system.
- 2: Preparation: goods/parcels get separated and oriented.
- 3: Identification: scanner identify goods/parcels and read out their destination.
- 4: Sorter: goods are distributed to their allocated output.
- 5: Accumulation area (Discharging): goods leave the sorting system.

In this paper the authors focus on the sorter itself and here on the in-feed process, where the ICMaS'12 contribution focused the discharging with tilt-tray-sorters

Fig. 3. Sortation system [1, 6].



**Fig. 4.** In-feed, mechanical solutions: **a** round belts, **b** stripe belts, **c** flexible angled-belt [1].

[6]. For details of other parts the reader may refer to literature [1].

Various different ways to design the automated infeed have been developed from those few successful manufacturers where Fig. 4 gives an overview.

The main task for the in-feed process is to secure

- a precise position;
- a precise orientation;
- the right speed with accelerating the good.

of the feeding goods overhandling on the conveyor. This is depending from the typ of the conveyor and therefore highly sophisticated, because the sorting system can only handle, what the in-feed provides, with respect to the system performance. The main challenges of the in-feed process can be identified as:

- different speeds of sorter in in-feed;
- a speed-component lateral to the component in sorter direction (v<sub>s</sub> in Fig. 10);
- high performance of sorting process (with i.e. 15.000 sortations per hour) and therefore high accuracy for the in-feed at high speed-levels.
- The core element of the in-feed is a flat or round belt – the in-feed-conveyor –, which carries, transports and

accelerates the piece good. Geometrical and dynamic parameters are matter to variation. So this belt is the main object of further modelling within various CAEapproaches as following.

## 3. CAE

CAE is not only dynamics simulation with multibody dynamics (MBD), but a very large field of different approaches, modelling physical behavior with a set of describing equations and their numerical solution. The main domains of CAE in engineering are shown in Fig. 5 and can be found within [5].

All of them can be represented in different software signal-flow-oriented domains. like systems (MATLAB/Simulink) or graphical library-based systems. All further comments refer to MBD-Systems. The great difference is in how one has to build the model, with one time deriving all governing equations exactly and bringing them to a numerical (or very rare analytical) solution. The other time powerful software-tools like MSC.ADAMS, ITI SimX, RecurDyn, Simpack or CADintegrated CAE-tools in all major CAD-systems enable a very easy way to model basic behavior. Herein a spring looks like a spring and has two "physical connectors" in difference to its governing equation, which powers the object in behind.

### 3.1. MBD modelling for conveyor belt drives

The in-feed-conveyor is normally a belt drive with two pulleys and tensioning device (Fig. 4). Much theoretical work has been done analytically and in respect to belt materials, to ensure a secure function [10]. The belt drive modelling in MBD and the main commercial systems therein is until now limited to traction belts where conveying is no matter. Special toolkits (Fig. 6) are commercial products to model dynamic load history for stress and fatigue analysis as well as belt dynamics with respect to pulley/belt design, some more sophisticated methods for tension-member drives – in parallel to FEMtechnologies – are in development i.e. for MSC.ADAMS [13].



Fig. 5. CAE domains in mechanical engineering (and logistics engineering).

These "drives" are modelled by transfer functions between all included parts and have no possibility, to act as a conveyor, as they only transfer dynamic parameters (moments, angular speeds,...) from one pulley to the other.

The in-feed-conveyor now has to carry loads on its tension member on the carriage side with interaction between the load and the belt via normal and friction forces. Because the SLAKE isn't important the following modelling is suggested, to model belt conveyors in logistics:

- a rigid body represents the carriage side of the conveyor;
- this conveyor is driven by an outer control via powering moment or dynamic constraints;
- the contact to the piece good is established via
  - o 3D-geometry-based-contacts (details in [6]);
  - characteristic points of contact, represented in CAD-geometry, to avoid plane surface/surface contact which is numerically unstable; reducing the parcel surface to "ideal" contact points;
- these contacts are activated/deactivated selectively, controlled by position measurement, to
  - o discharge the good from the conveyor;
  - o overhand to another conveyor;
  - *Note*: the conveyor itself has not any contact to other bodies, beside the carrying goods.

So in case of the in-feed, two rigid bodies are intersecting each other with no contact in between (Fig. 7). The piece good is transferred from one conveyor to the other by selectively (de)activating contacts. This procedure makes much effort in modelling, but is by state of the art of simulation tools the only way to model the conveyor. Another approach, via flexible or incremental belt bodies has been chosen but withdrawn because of modelling effort and computation time.

### 4. MODELLING OF THE IN-FEED

Besides there are some necessary adaptions for modelling belt drives in MBD from 3.1, there is another big challenge to implement: the piece good and it's contact description to the conveyor.

odules		
Gears Module		
Beits Module		
	<ul> <li>The Belts module is designed for engineers who need to predict the impact of the design and dynamic behavior of pulley-belt systems, such as transmission ratio, tension and load prediction, compliance studies, or belt dynamics, on the overall system performance.</li> <li>Choose the belt type with the selection of Poly-V Grooved belt. Trapecoidal Toothed belt and Smooth belt</li> <li>Apply 2D Links modeling method to calculate the contact forces between the segments and pulleys when the asis of rotation is parallel to one of the global axes.</li> <li>Use Genmetry settings to define the location and geometric parameters of your pulleys.</li> <li>Apply tensioner pulley to the belt system to take up the estra slack and control the rooting of the belt.</li> <li>Use actuation weard to apply force or motion to any pulley in the belt system.</li> </ul>	
	<ul> <li>contact forces between the segments and pulleys when the axis of rotation is parallel to use of the global axes.</li> <li>Use Genmetry settings to define the location and geometric parameters of your pulleys.</li> <li>Apply tensioner pulley to the belt system to take up the extra slack and control the rotating of the belt.</li> <li>Use actuation weard to apply force or notion to any pulley in the belt system.</li> </ul>	

Fig. 6. Factsheet of MSC.ADAMS/Machinery – Beltdrive [4]



Fig. 7. in-feed with the conveyor- model from 3.1, and the conveyor-piece good contact from 4.1 with characteristic points of contact, represented in CAD-geometry.

Therefore one has to take a very detailed look at contact formulation, which can be found in [6] to get performing simulations. As in case of the conveyor-piece good contact brings two plane surfaces together. There is one main aspect to consider. Two plane surfaces do not have a unique solution to define contact points, which is what the typical contact-statements in MBD expect. So the following approach has been chosen.

#### 4.1. MSC.ADAMS - MBD approach 3D

Modelling the piece good-conveyor interaction via i.e. the MSC.ADAMS CONTACT statement [4] it was necessary, to provide at least one uneven surface via CAD-geometry - what the parcel or the conveyor is in real! Thus the parcel got i.e. nine half-spheres at governing positions, to force contact points and tracks therein (Fig. 7) – contact regions, theory in [3]. Using a non uniform distribution of mass inside the parcel, a real world contact is simulated the better, the more halfspheres are modelled. This is in direct conflict with underlying modelling effort and simulation duration, where the number of nine contact regions could be identified as sufficient, also in respect to the analytical approach, which can consider ideal plain surface/surface contact (chap. 4.2) to validate the discrete approach via halfspheres.

Modelling the conveyor the approach from 3.1 was chosen and combined with the piece good-contact.

The overall MSC.ADAMS MBD simulation of the in-feed process is depicted in Fig. 7 with:

- Two rigid bodies representing the conveyors (chap. 3.1).
- The in-feed of the parcel with discrete contact formulation (chap. 4.1).
- A nonlinear contact statement at each half-sphere contact region [6], modelling a nonlinear visco-elastic material behavior of i.e. carton-rubber or softer or harder contacts depending on carried goods and belts.

Thus the model is performing, it was used to analyze various scenarios with special respect to dynamic behavior and size of contact forces of the in-feeded goods (Figs. 9, 10, ans 11).

## 4.2. 2D-MBD (Modeling)

A way to avoid problems caused by full 3D contact formulations mentioned before is to use a reduced 2D representation [11]. That means the parcel cannot lift of from the conveyor. This assumption allows a relative simple description of the feed-in process.

By separating the contact surface (Fig. 8) into a certain number of square elements, the base for further numerical implementations is created. The single elements are denoted by the indices *i* (direction  $\eta$ ) and *j* (direction  $\xi$ ). The size of *ge* is affecting the accuracy of the simulation results and the calculating time. The normal forces  $N_{ij}$  and the friction forces  $R_{ij}$  are applied at the midpoint of each element.

For implementing static and dynamic friction in the MBD-Model a velocity proportional definition of the friction coefficient  $\mu$  is selected (STEP-function [6]).



Fig. 9. GUI of the 2D-approach for the in-feed.

The differential equations to calculate center of gravity accelerations are obtained by the use of Newton's second law

$$\ddot{x} = \frac{R_x}{m} \quad \ddot{z} = \frac{R_z}{m} \quad \ddot{\phi}_y = \frac{M_y}{J_y}, \tag{1}$$

The entire friction force R is calculated by adding all single element friction forces  $R_{ij}$ . The summation of the single element friction forces follows:

$$R_{x} = \sum_{i=1}^{anb} \sum_{j=1}^{anx} R_{xij} \quad R_{z} = \sum_{i=1}^{anb} \sum_{j=1}^{anx} R_{zij}$$
(2)

The moment  $M_y$ , which is caused by friction forces  $R_{ij}$ , is obtained analogical:

$$\begin{bmatrix} r_{xij} \\ 0 \\ r_{zij} \end{bmatrix} \times \begin{bmatrix} R_{xij} \\ 0 \\ R_{zij} \end{bmatrix} = \begin{bmatrix} 0 \\ M_{yij} \\ 0 \end{bmatrix}; M_y = \sum_{i=1}^{anh} \sum_{j=1}^{anx} M_{yij}$$
(3)

The absolute and relative velocities for each element midpoint, necessary for evaluating the friction forces, are:

$$\begin{bmatrix} \dot{x} \\ 0 \\ \dot{z} \end{bmatrix} + \begin{bmatrix} 0 \\ \dot{\phi}_{y} \\ 0 \end{bmatrix} \times \begin{bmatrix} r_{xij} \\ 0 \\ r_{zij} \end{bmatrix} = \begin{bmatrix} v_{xij} \\ 0 \\ v_{zij} \end{bmatrix}; \quad (4)$$

$$\begin{bmatrix} v_{xij} \\ 0 \\ v_{zij} \end{bmatrix} - \begin{bmatrix} v_{Mx} \\ 0 \\ v_{Mz} \end{bmatrix} = \begin{bmatrix} v_{rxij} \\ 0 \\ v_{rzij} \end{bmatrix} \text{ or } \begin{bmatrix} v_{xij} \\ 0 \\ v_{zij} \end{bmatrix} - \begin{bmatrix} v_{Sx} \\ 0 \\ v_{Sz} \end{bmatrix} = \begin{bmatrix} v_{rxij} \\ 0 \\ v_{rzij} \end{bmatrix} (5)$$

Using the Coulomb friction model (friction coefficient  $\mu_{ij}$ ), the element friction forces  $R_{ij}$  are read as follows:

$$\begin{bmatrix} R_{xij} \\ 0 \\ R_{zij} \end{bmatrix} = N_{ij} \cdot \mu_{ij} \left( \sqrt{v_{rxij}^2 + v_{rzij}^2} \right) \cdot \begin{bmatrix} -v_{rxij} \\ 0 \\ -v_{rzij} \end{bmatrix} \cdot \frac{1}{\sqrt{v_{rxij}^2 + v_{rzij}^2}} \quad .$$
(6)

The advantages of the 2D - model are:

- proper numerical handling (important for computational implementations);
- high accuracy of results (realistic implementation of friction effects);
- it is possible to consider roller conveyors or other belt configurations;
- extendable for non- block shaped packets;
- implementation of non-constant surface pressure distributions between packet and belt possible.

## 4.3. Numerical Implementation and results

The software to simulate the merging procedure is written in MATLAB Fig. 9 shows the GUI of the program. There are different options for simulating belt conveyors, roll conveyors and strip merges [12].

Output of the program are all relevant data for analysing the motion process during feed-in. For that reason packet position and velocity are evaluated. Friction forces and friction moments are crucial for understanding the merging procedure. They are calculated for every time step. (Fig. 11). Fig. 10 illustrates the flow diagram of the program and the trace curves of a parcel during the feed-in process evaluated by the software.

The software allows engineers a fast and safe dimensioning process of merges. Fig.11 shows specific results and for instance the variation of friction coefficients for a precise performing feed-in process. All this can be used to shorten development times by virtual testing and Design of Experiments (DoE).

#### 4.4. Validation – selected results

As the 2D and the 3D model represent the same physical behavior but with slightly different modelling, taking different aspects into account, the results can be compared selectively and the models used for different depths and interests in investigation (see chap. 5).

Interesting results for system performance as well as for validation are:

- Friction forces good-conveyor: to examine the behavior and possible damage to the piece goods
- Speeds of in-feeding goods: to secure exact matching the pre-defined in-feed position/orientation on the main conveyor for high performance operation of the sorting system.

The smaller the distance between in-feeded goods becomes the higher the sorting performance will be. The main constraint for safe in-feed can be stated with:

$$v_s = \frac{v_M}{\cos(\alpha)}.$$
 (7)

With  $v_s$  sorter main conveyor speed and  $v_m$  merge speed with  $\alpha$  as angle between sorter and merge. Therein all dynamic effects from friction and mass have influence on a non constant  $v_m$  during overlapping to  $v_s$ .



Fig. 10. Flow diagram and trace curves of the feed-in process.



Fig. 11. Influence of friction coefficient on feed-in.

Now Fig. 12 shows the friction forces ( $R_x$ ,  $R_z$  in x and z direction) and speeds of the two different models over time for validation.

The speeds of the in-feeded goods show quite equal behavior as promised in prior work [11].

With those two different approaches for modelling the in-feed performing the same quality of results in the defined scope of interest, the two models can be used selectively for different tasks in investigation to maximize the simulation performance in respect to:

- computation time and accuracy;
- necessary effort in adaption of parameters and geometries;
- more global scenarios with connecting the in-feed to other simulation models (i.e. roller-conveyor, sorting mechanisms,...);

Friction forces match from both models with the following findings:

- The ADAMS (3D) model behaves more "discrete" because of switching on contacts selectively.
- It also shows some spikes, resulting from the representation over only four contact points, where the 2D model uses a much higher discretization of the surface-surface contact.
- The time behavior and the overall friction force work is equal.

## 5. COMPARISON OF 2D AND 3D APPROACH OF THE IN-FEED PROCESS

Chapter five now works out the differences in modelling as an overview in Table 1, to provide insights in how to use which approach in case of modelling the in-feed and similar modelling tasks in material handling simulation of piece goods. It shows how to optimize the in-feed by the use of the 2D and 3D models.



**Fig. 12**. in-feed with the 2D and 3D in-feed model. Friction forces and speeds in *x* and *z* direction.

Table 1

category		2D	3D (ADAMS)		
	equations of	explicit	implicit		
	motion				
	geometries	idealized	real CAD		
ng	contacts	various formu-	see CONTACT		
leli	<u> </u>	lations	statement [6]		
noc	effort	high	medium/high		
-	adaptivity	very last	Tast voru high		
adaptivity		nartial	full		
	ability	partial	Tun		
	masses	freely ad	liustable		
	load distri-	partially varia-	full flexibility/		
ers	bution	ble	interconnection		
neto	speed	freely ac	ljustable		
ran	feeding	freely adjustable			
pa	angle				
lell	friction	dependency of sliding speed			
nod	contact	(no stiction: CON	IACI statement)		
ц ц	contact	lomb friction	CONTACT		
		only)	continer		
	software	math. or numer-	various MBD		
	Ū.	ical tool (Sim-	commercial and		
		ulink)	free tools		
50	numerical	free	predefined		
vin	method		solver and		
sol		6	robust		
	duration	very fast	fast		
	autom. per-	only by user	built in		
	(DoF)	written routilies			
-	visuali-	only by user	within package		
ing	zation (vid-	written routines,	r		
cess	eo)	additional effort			
roe	quick check	possible, addi-	easily by as-		
st p	and proof of	tional effort	sessment of		
od	concept				
	one parcel	built in			
	> one par-	not appropriate	possible		
	cel		P		
	interaction	hardly imple-	all possibilities		
	with further	mentable			
	machinery				
	(parcels)	1	-11		
	impacis overhand-	mentable	an possibilities		
	ling to/from	mentable			
SSS	conveyors				
000	2				
I pr	detailed	hardly imple-	nossible even		
eec	forces on	mentable	stress recovery.		
in-f	goods		~~~~~		
	discrete	impossible	possible		
	events				
	(dumping)				
	quali-	mainly depending on discretization			
	ty/accuracy	of contac	et surface		
	oj results further	reduced models	all MBD func		
	juriner jn-food	(via analytical	tionality availa-		
	technologies	approaches)	hle		
	(rollers)	"PProuenes)	010		

Overview	of potentialities and	parameter	ranges	within	the
	2D and 3	D model			

Using the 2D and 3D model adequately makes the infeed process better performing in real scenarios, as certain exotic variations and combinations of parameters could have never investigated on real test-stands as well as the number of overall simulation runs and scenarios has been much higher in the virtual world. So this paper contributes to make engineering tasks in material handling development more "state of the art", which is a declared mission of the Institute of Logistics Engineering in Graz.

## 6. SUMMARY

This paper compares two different approaches in modelling the highly dynamic process of the in-feed, wherein both methodologies show results accordingly. An overview of possibilities in general use of these methods concludes the paper.

Ongoing and further research at the Institute of Logistics Engineering will provide a "conveyor-toolbox" within CAE for common material handling technology. This box can be used to build CAE – models in short tim, with high accuracy by basing on submodules. As a concluding step it's planned to replace or minimize physical test-stands by only performing CAE test runs.

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